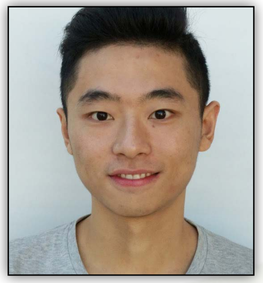
CVPR SEATTLE WASHINGTON JUNE 16-18 2020

CvxNet

Learnable Convex Decomposition


Boyang Deng


Kyle Genova


Sofien Bouaziz


Soroosh Yazdani


Geoffrey Hinton

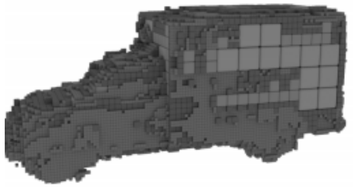

Andrea Tagliasacchi

Google Research

Family of 3D representations

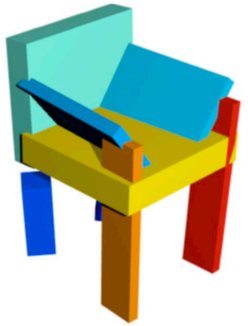
Tatarchenko et al. 2017

{voxels}



Tulsiani et al. 2017

{boxes}



Groueix et al. 2018

{patches}

Genova et al. 2019

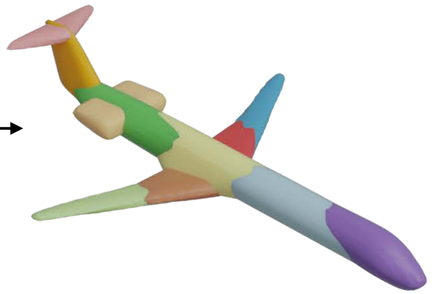
{gaussians}

Mescheder et al. 2019

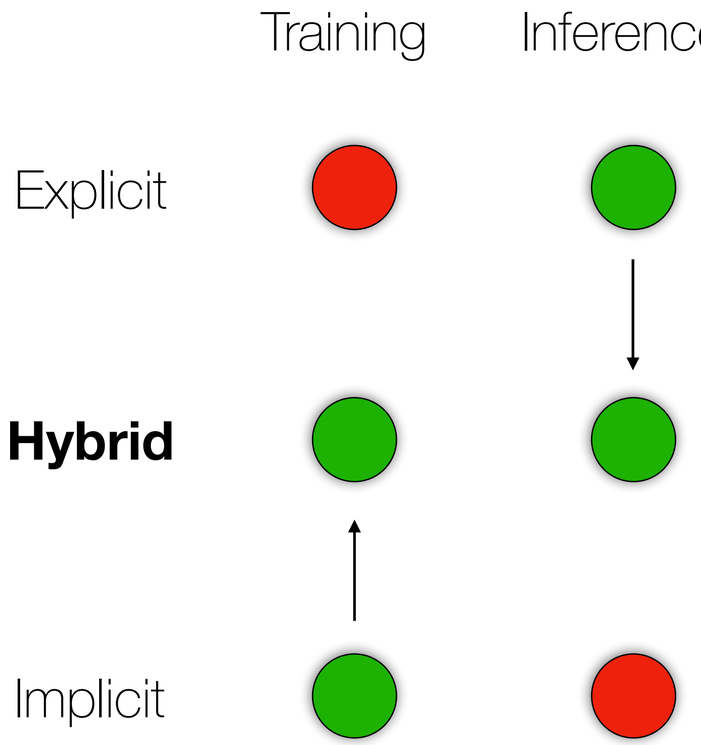
implicits

Deng et al. 2020

{convexes}



What is the «best» 3D representation?



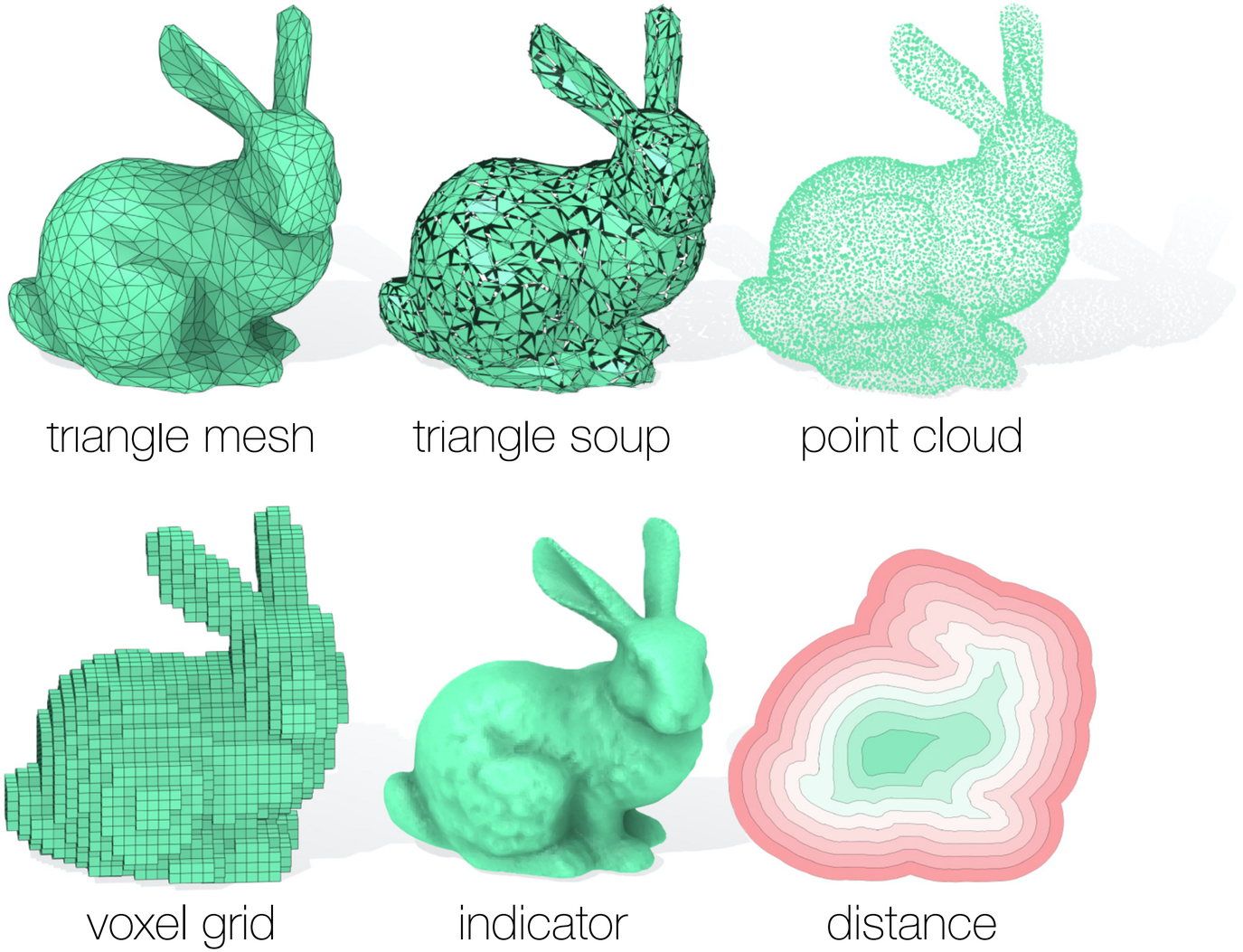
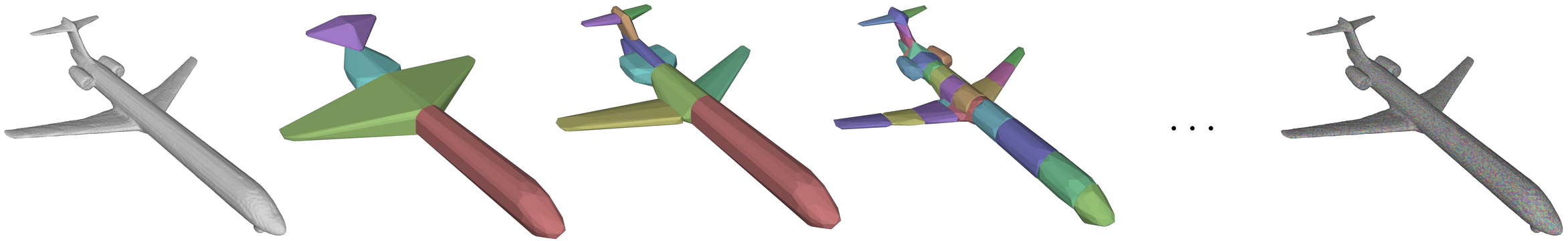


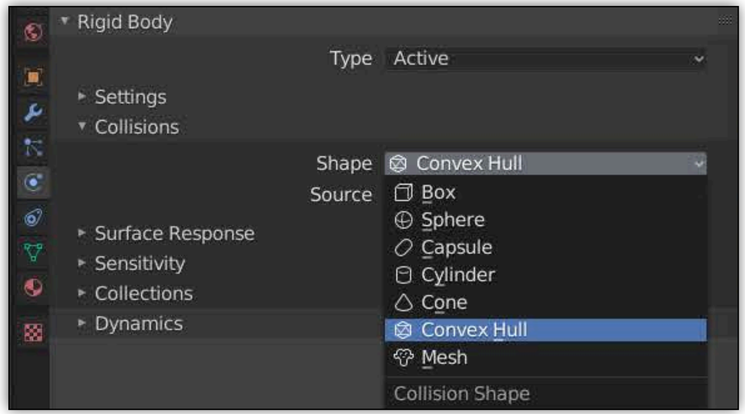
Image courtesy of Barill et al. «Fast Winding Numbers for Soups and Clouds» SIGGRAPH 2018

Convexes: why are they relevant?



input — K=4 — K=8 — K=32 — universal approximators — K=∞ →

rigid body physics →



Convex Hulls (standard)

Meshes (the «wild west»)

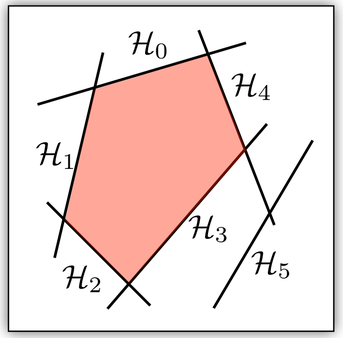
decomposition computed by «v-hacd» – https://github.com/kmammou/v-hacd

Universal approximator of convex domains

$\cdots$ $\mathcal{E}_\omega$

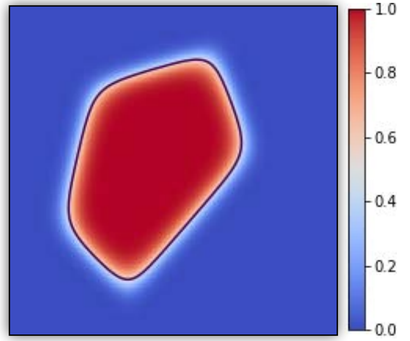
input: half-spaces tensor

$$\begin{bmatrix} n_0^x & n_0^y & d_0 \\ n_1^x & n_1^y & d_1 \\ \cdots & \cdots & \cdots \\ n_5^x & n_5^y & d_5 \end{bmatrix} \equiv \begin{bmatrix} \mathcal{H}_0 \\ \mathcal{H}_1 \\ \cdots \\ \mathcal{H}_5 \end{bmatrix} \equiv$$

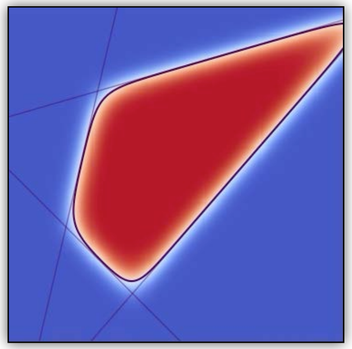


$\mathcal{C}(\mathbf{x}|\boldsymbol{\beta})$

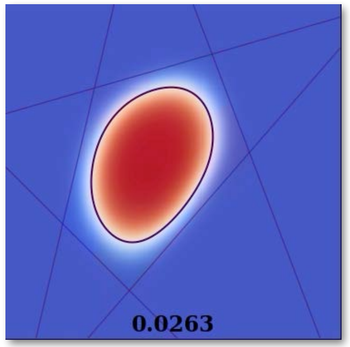
output: function



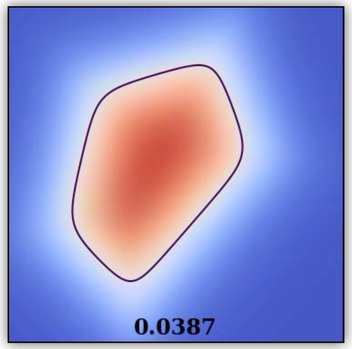
$$\overbrace{\text{Sigmoid}(-\sigma\text{LogSumExp}\{\delta(\mathbf{n_h}\cdot\mathbf{x}+d_h)\})}$$



permutation invariance

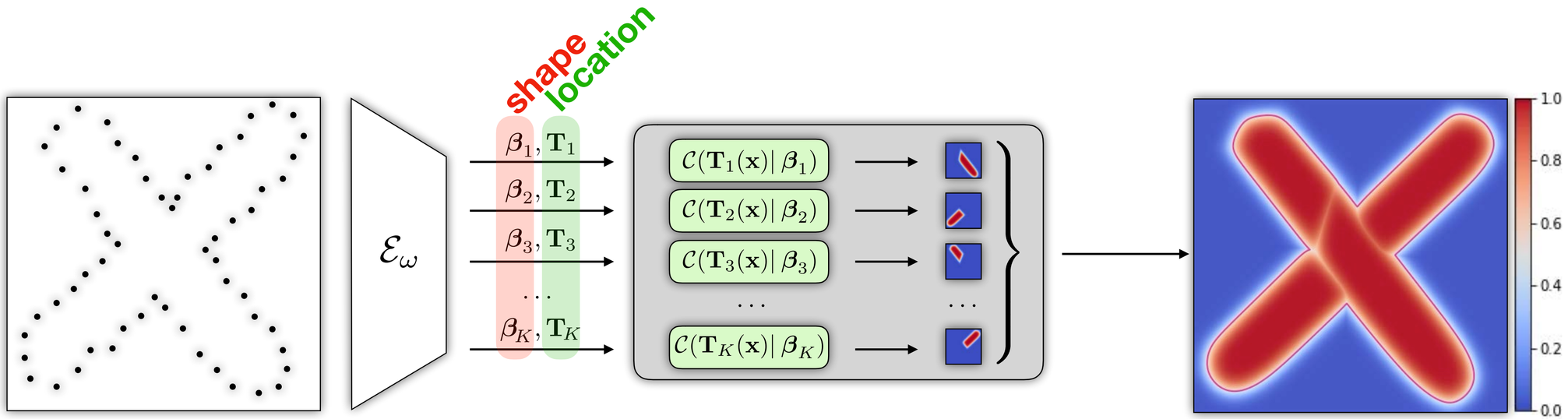


δ controls smoothness

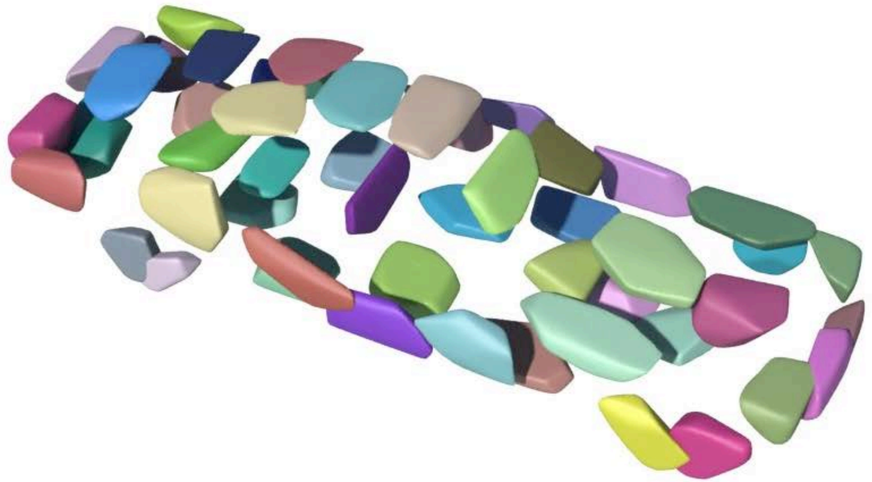


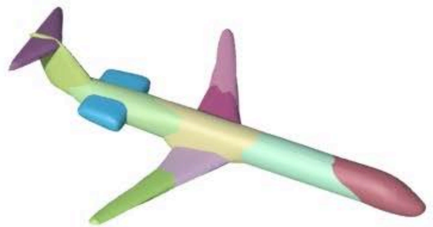
σ controls indicator dropoff

… and non-convex domains!

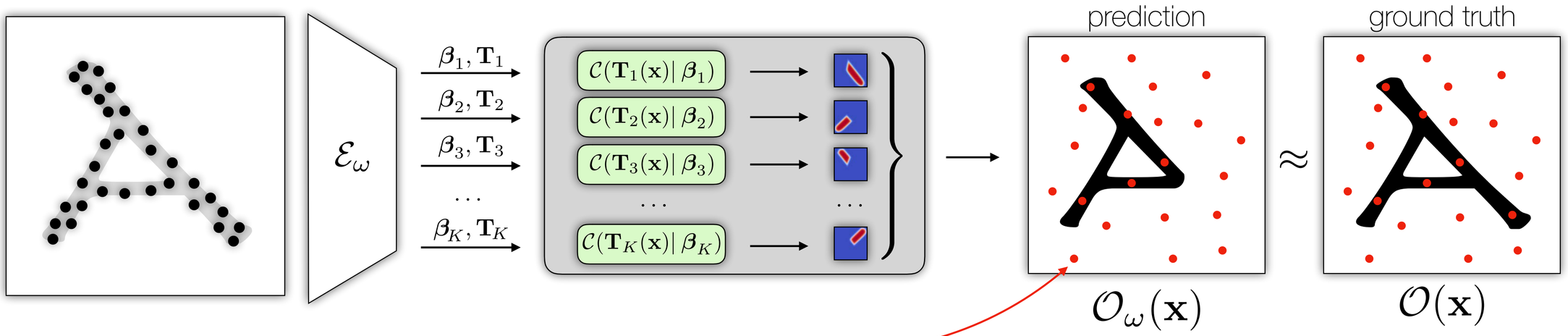


$$\mathcal{O}_\omega(\mathbf{x}) = \max_k \{\mathcal{C}(\mathbf{T}_k(\mathbf{x})|\boldsymbol{\beta}_k)\}$$





Implicit functions @ training time



$$\mathcal{L}_{\text{approx}}(\omega) = \mathbb{E}_{\mathbf{x}\sim\mathbb{R}^2} \|\mathcal{O}_\omega(\mathbf{x}) - \mathcal{O}(\mathbf{x})\|^2$$

$$\mathcal{L}_{\text{decomp}}(\omega) = \mathbb{E}_{\mathbf{x}\sim\mathbb{R}^3} \|\text{relu}(\text{sum}_k\{\mathcal{C}_k(\mathbf{x})\} - \tau)\|^2$$

$$\mathcal{L}_{\text{unique}}(\omega) = \frac{1}{H}\Sigma_h \|d_h\|^2$$

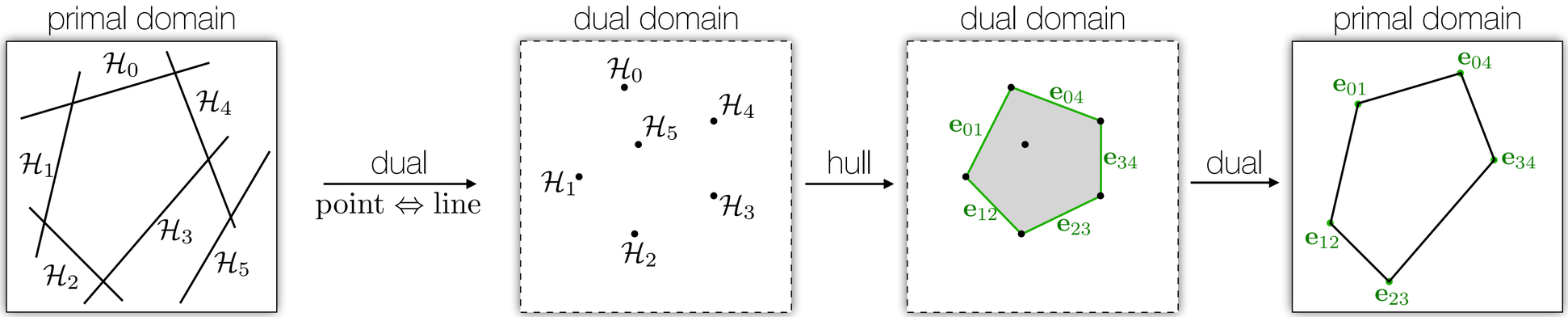
$$\mathcal{L}_{\text{merged}}(\omega) = \frac{1}{K}\Sigma_k \frac{1}{N}\Sigma_{\mathbf{x}\in\mathcal{N}_k} \|\text{ReLU}(\Phi_k(\mathbf{x}))\|^2$$

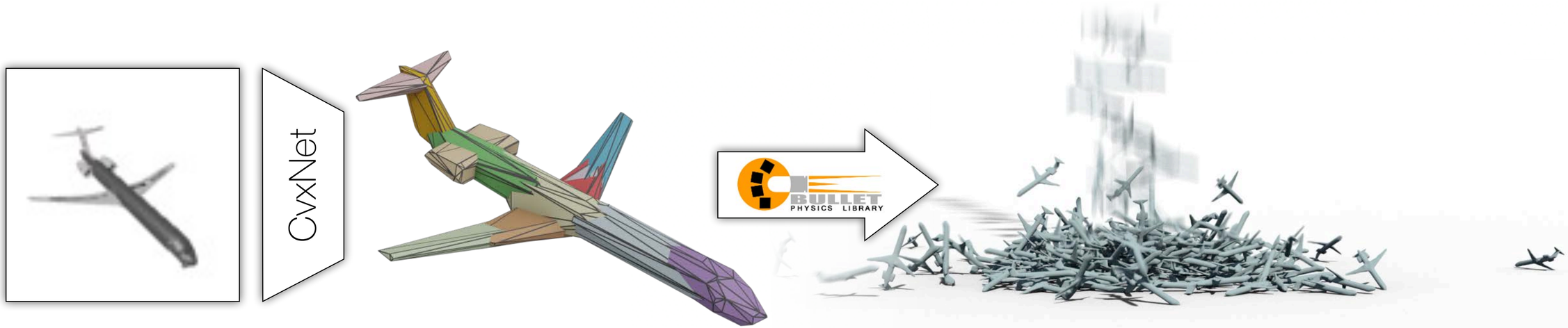
convexes should not overlap

only one way to represent a convex

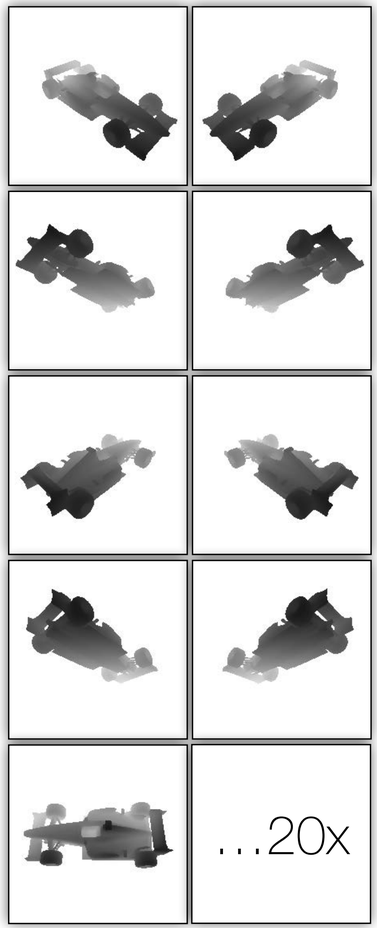
prevents vanishing gradients

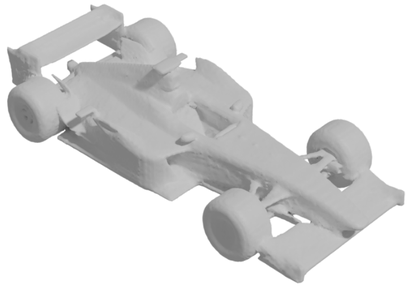
Polygonal meshes @ inference time



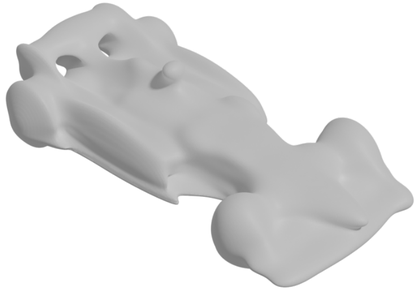


Multi view reconstruction – {Depth}→3D

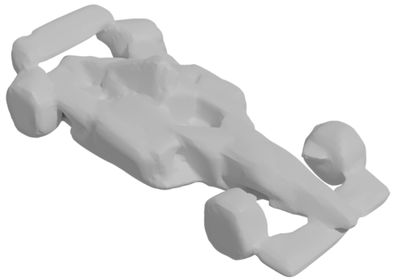




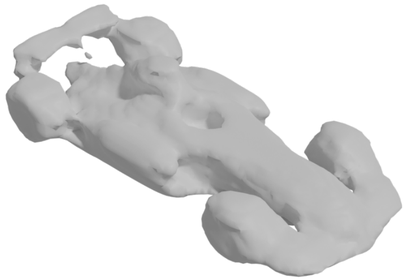
Ground Truth
Mesh



SIF
[Genova et al. 2019]



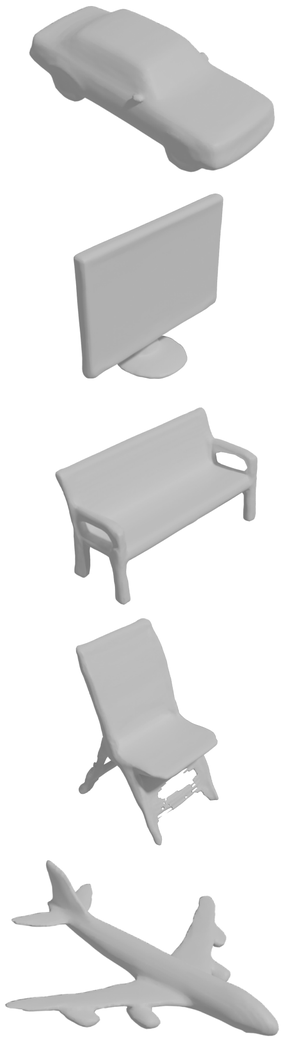
CvxNet
[Deng et al. 2020]



OccNet
[Mescheder et al. 2019]

Category	F-Score		
	OccNet	SIF	CvxNet
airplane	79.52	71.40	**84.68**
bench	71.98	58.35	**77.68**
cabinet	71.31	59.26	**76.09**
car	69.64	56.58	**77.75**
chair	63.14	42.37	**65.39**
display	63.76	56.26	**71.41**
lamp	**51.60**	35.01	51.37
speaker	58.09	47.39	**60.24**
rifle	78.52	70.01	**83.63**
sofa	69.66	55.22	**75.44**
table	68.80	55.66	**71.73**
phone	85.60	81.82	**89.28**
vessel	66.48	54.15	**70.77**
mean	69.08	59.02	**73.49**

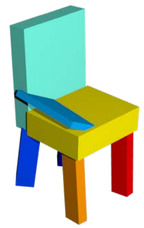
Single view reconstruction (SVR)



N/A

N/A

N/A



Input Image

Ground Truth Mesh

CvxNet [Deng et al. 2020]

AtlasNet [Groueix et al. 2019]

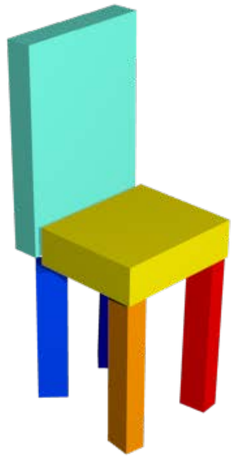
OccNet [Mescheder et al. 2019]

Structured Implicits [Genova et al. 2019]

Volumetric Primitives [Tulsiani et al. 2017]

Shape approximation – comparisons

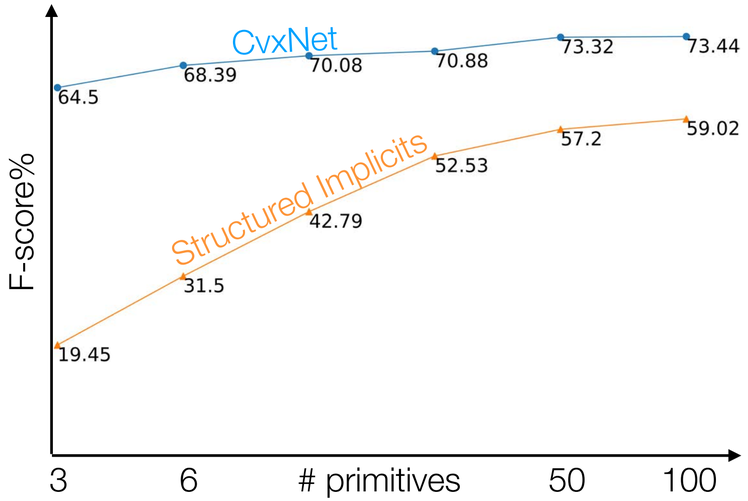
Ground Truth
Mesh

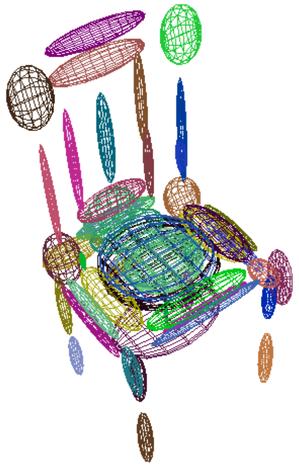


Volumetric Primitives
[Tulsiani et al. 2017]

CvxNet
[Deng et al. 2019]

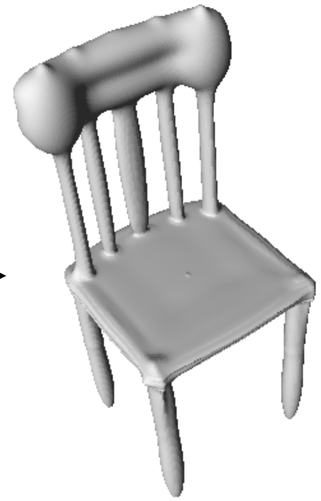
«union»

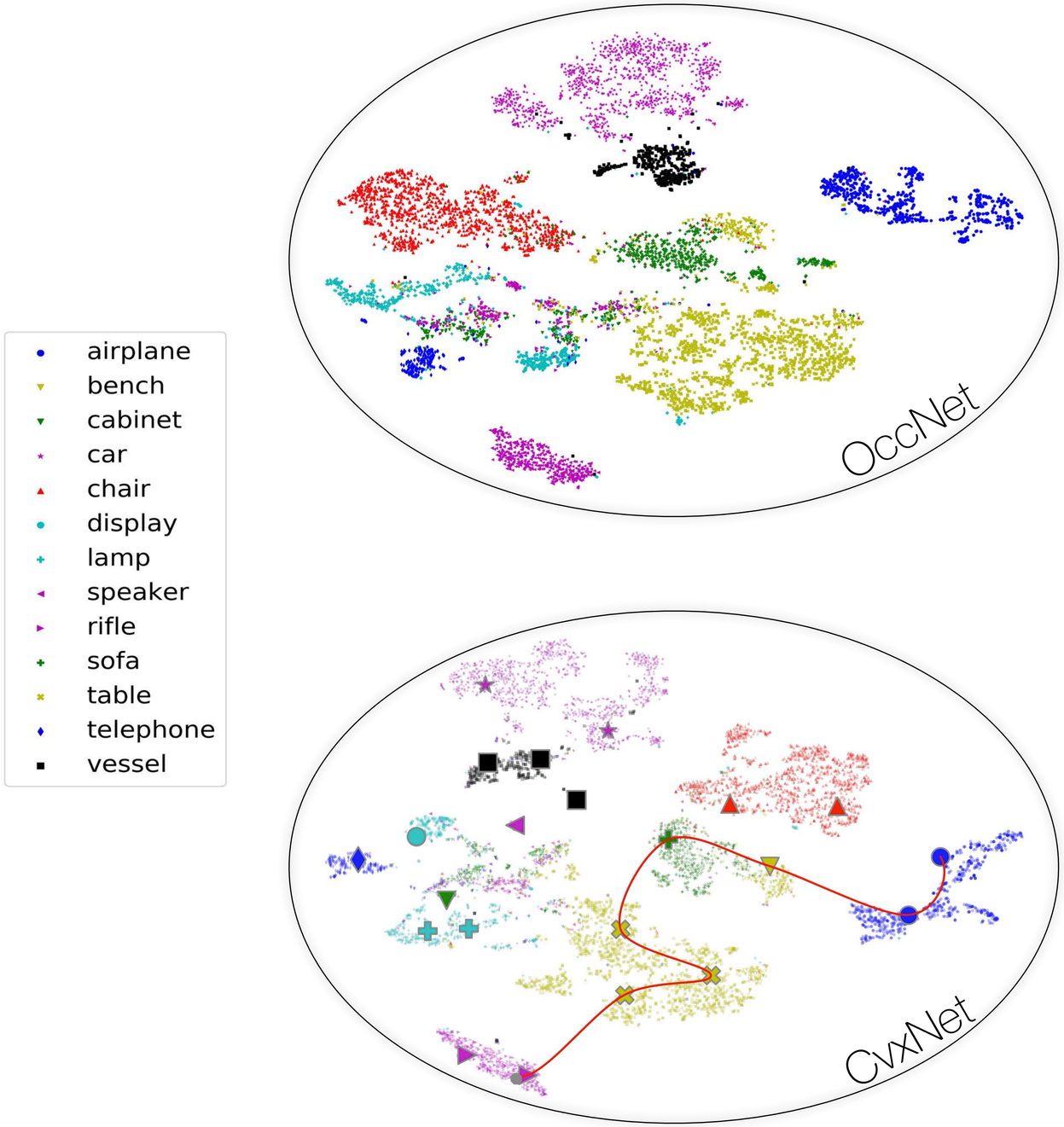


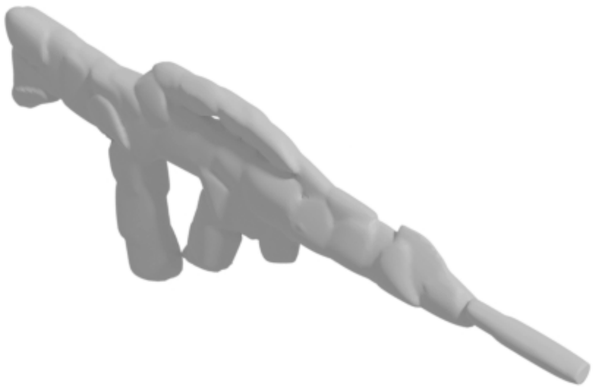


Structured Implicits
[Genova et al. 2019]

«structuring»



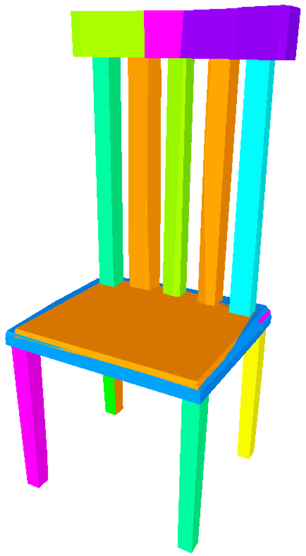

airplane
bench
cabinet
car
chair
display
lamp
speaker
rifle
sofa
table
telephone
vessel
OccNet
CvxNet



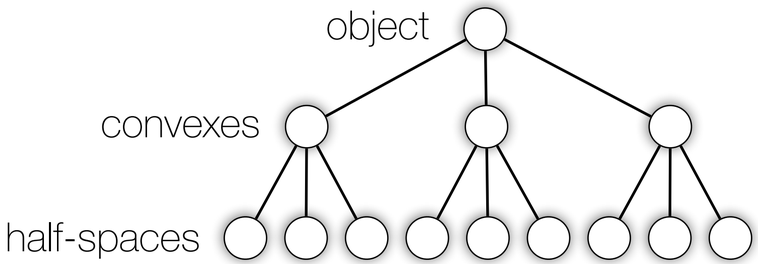
Related work @ CVPR 2020

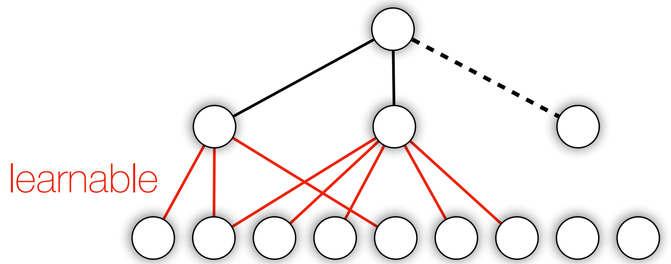
Deng et al. «CvxNet»
smooth convexes, **fixed** graph

focus



Chen et al. «BSP-Net»
graph learning, **sharp** details





CvxNet
Learnable Convex Decomposition

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Google Research

cvxnet.github.io